Security-Constrained Unit Commitment with Natural Gas Pipeline Transient Constraints

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Abstract—The interdependencies of power systems and natural gas networks have increased due to the additional installations of more environmental-friendly and fast-ramping natural gas power plants. The natural gas transmission network constraints and the use of natural gas for other types of loads can affect the delivery of natural gas to generation units. These interdependencies will affect the power system security and economics in day-ahead and real-time operations. Hence, it is imperative to analyze the impact of natural gas network constraints on the security-constrained unit commitment (SCUC) problem. In particular, it is important to include natural gas and electricity network transients in the integrated system security because the impacts of any disturbances propagate at two distinctly different speeds in natural gas and electricity networks. Thus, analyzing the transient behavior of the natural gas network on the security of natural gas power plants would be essential as these plants are considered to be very flexible in electricity networks. This paper presents a method for solving the SCUC problem considering the transient behavior of the natural gas transmission network. The applicability of the presented method and the accuracy of the proposed solution are demonstrated for the IEEE 118-bus power system, which is linked with the natural gas transmission system and the results are discussed in the paper.

Index Terms—Natural gas transients, SCUC, gas transmission network,

I. NOMENCLATURE

A. Set and indexes

\[ i \] Index of thermal generating units.
\[ j \] Index of contingency.
\[ NG \] Number of thermal units.
\[ k, y, q \in g \] Index of node in natural gas network.
\[ p, q \in m \] Index of bus in power transmission network.
\[ t \] Index of hour.
\[ T \] Number of hourly periods.
\[ x \] Index of length through pipeline.
\[ so \] Index of natural gas storage.
\[ sup \] Index of natural gas supplier.
\[ pip \] Index of natural gas pipeline.

B. Variables

\[ \pi \] Pressure at the nodes [bar].
\[ I \] Binary variable indicating ON/OFF status of units.
\[ n, f \] Startup/Shutdown binary indicator.
\[ P, \dot{P} \] Generation dispatch of units [MW].
\[ P_{es} \] Electrical load shedding [MW].
\[ Q \] Natural gas flow [MSm³].
\[ Q_{con} \] Flow of compressor [MSm³].
\[ Q_{in}, Q_{out} \] Input/output volume of gas storage [MSm³].
\[ \theta \] Voltage angle of power system buses [rad].
\[ \gamma \] Voltage angle of phase shifter [rad].
\[ a \] Linear cost of generating units.
\[ b \] Constant cost of units.
\[ c \] Sound velocity [m/s].
\[ D \] Diameter of pipeline [m].
\[ DR, UR \] Down and up ramp rate of units.
\[ E \] Storage useful inventory.
\[ E_{\min}, E_{\max} \] Min/Max capacity of gas storage [MSm³].
\[ ER \] Output rate of gas storage.
\[ SR \] Max output of natural gas storage facilities [MSm³].
\[ l \] Length of pipeline [m].
\[ MxFlow \] Maximum flow rate of power transmission.
\[ P_D \] Power Demand [MW].
\[ F_{\max}\] Maximum natural gas allocation to gas fired units.
\[ \pi_{\min}, \pi_{\max}\] Min/max pressure of nodes in gas network [bar].
\[ P_{\min}, P_{\max}\] Min/max power output of generators [MW].
\[ Q_G \] Gas load [MSm³].
\[ Q_{\min}, Q_{\max}\] Min/max output flow of supplier [MSm³].
\[ R \] Spinning reserve [MW].
\[ SU, SD \] Fuel consumed for starting up and shutting down units.
\[ S \] The specific gravity of gas, it is the ratio of densities between gas and air.
\[ \varepsilon \] Compressibility factor.
\[ \phi_f \] Friction factor of gas transmission.
\[ \rho \] Density of fluid (gas=0.7165).
\[ \alpha \] Compression factor.
\[ \sigma \] Contracted fuel price [$/MSm³].
\[ \omega \] Electricity load shedding price [$/MW].

II. INTRODUCTION

In the recent decades, the share of natural gas power plants in supplying power system loads has increased significantly. It is expected that the capacity of natural gas power plants would be increased by 110% between 2012 to 2040 [1].
Various factors have contributed to the fast development of natural gas power plants as compared to other electricity sources including higher efficiency, lower pollution in terms of emitting NOx, SOx and other carbon pollutants, fast installation process, higher flexibility, etc. [2].

Natural gas power plants are large consumers of natural gas transmission system and large deployments of such plants can create serious issues for the natural gas network. For example, large consumptions of natural gas for supplying the static loads such as residential applications could reduce the pipeline pressure and, the reduction of natural gas supply to power plants [3].

Gas travels at a much lower velocity than electricity and due to its compressibility can be stored in pipelines. Dynamic approximations, involving gas compressibility and velocity, represent longer stabilization times required to respond to changes in gas loads and disruptions. It is undeniable that consideration of these approximations is necessary for providing the grade of flexibility and reliability that power systems require from gas. Thus, it is critical to consider natural gas network constraints and pipeline transients in power system studies.

The integrated studies of power systems which consider the effect of natural gas networks have been emphasized in the existing literature. Much of these studies have investigated the integration of natural gas systems in security constrained unit commitment (SCUC). In [4], natural gas transmission network has been implemented in the optimal power flow calculation. In general, considering natural gas transmission constraints emerges in multilateral planning of transmission systems and different types of energy hubs [5].

Various aspects of natural gas networks were introduced in power system studies. In [6], a low-carbon electricity network was investigated and in [7] energy market participation strategy was analyzed. A security constrained short-term generation planning with natural gas network was presented in [8] in which the Monte Carlo scenarios generated random contingencies on both networks. In [9], a bi-level optimization of natural gas consumption in SCUC was presented in which the natural gas network was modeled in static mode using a genetic algorithm. In [10], natural gas network was linearized and solved by the Newton–Raphson method. In [11], the variability of wind energy was formed by the quick ramping capability of natural gas units, and Benders decomposition was adopted to check the natural gas transmission feasibility.

In [12], dynamic energy flow was optimized by different response times of natural gas and power systems. The transient response of high-pressure natural gas flow in transmission pipelines was addressed in [13] and [14], where one-dimensional flow of compressible fluid was modeled numerically. In [15], natural gas network limitations were modeled as a sub-problem in SCUC using Weymouth equations. In addition, the dynamic model of natural gas network based on determining of mass flow by modeling the gas traveling velocity, compressibility and gas pressure was implemented in SCUC [16]-[17].

The transient natural gas behavior was presented based on the set of partial differential equations (PDEs) in [18] which could pose a convergence problem in a reasonable time scale specially in the short-term power system planning where the transient behavior of the natural gas network would be more effective. In addition, exploring a reasonable solution in a ringed natural gas network could not be easily realized.

The finite difference techniques and the PDEs both in space and time can be used for the transient behavior of the natural gas in the pipe, so the behavior of the natural gas in each time step is calculated by data of the previous time step. Solving all PDEs in space and time all around the network for the transient behavior of the natural gas in the pipelines is an extremely time consuming process. The proposed model could check the feasibility of the transient behavior of the gas network by some new constraints. Such as other control systems, changing the inputs will onset the other equations.

SCUC is considered a large-scale optimization problem and introducing a set of differential equations as additional constraints to represent the transient behavior of natural gas transmission network would increase the complexity of the power system scheduling problem. In some studies, a new linear steady state model of natural gas transmission network is introduced using the Weymouth equations [19].

The increasing penetration of variable renewable energy would mandate the use of fast response and flexible natural gas plants in constrained electricity and natural gas networks [20]. The corresponding variability and the flexible operation of natural gas units, in response to variability, could initiate sudden changes in the natural gas network and affect the transient behavior of natural gas network [21].

However, the transient behavior of security-constrained natural gas network in short-term power system studies have not been widely addressed in the literature. Accordingly, we formulate the electrical analogy in this paper to consider the transient behavior of a natural gas network.

This paper seeks to model an equivalent circuit for the natural gas transmission network. The problem is solved as an electric circuit in which a power flow method is applied to an equivalent circuit of natural gas transmission pipelines. According to the transient state in the equivalent electric circuit of natural gas network, main parameters that indicate transient behavior of natural gas network could be obtained such that a certain set of constraints could be added to check the security of natural gas transmission systems in transient state. Subsequently, the natural gas network can be controlled in both transients and steady states. The modeling of the transient behavior of natural gas will be presented as a set of constraints that could be added to the Weymouth equation to check the transient stability of the gas network alongside the steady state mode of the natural gas pipeline grid.

The rest of this paper is organized as follows: Section III proposes a transient model for natural gas transmission network which is based on electrical analogy. The mathematical formulation of SCUC with natural gas transmission network is presented in Section VI. The numerical studies for the IEEE 118-bus power system with 14-node natural gas transmission system is presented and analyzed in Section V to demonstrate merits of proposed model. Finally, the paper is concluded in Section VI.

### III. ELECTRICAL ANALOGY OF NATURAL GAS FLOW

Natural gas is extracted from wells in different areas and then collected and processed via a gathering system.
Processed natural gas is often transported through constrained pipeline networks to consumers which impose additional complexity to the natural gas flow delivery [22].

A. Electrical analogy of the natural gas pipelines

All natural gas flow equations in transient state are derived from three basic laws of mass and energy conservations and momentum [23]. These equations include mass continuity, amount of movement and energy, and an ideal natural gas status. An equivalent model of the gas networks has been presented in [24], solving the three main laws for transmission of the natural gas by replacing them with a set of equations in time and space. Therefore, they divided the pipeline to lots of small pipes and solved them along the length. In this paper, an equivalent electrical circuit has been drawn based on these three main laws and it is solved by using similar methods in the power transmission networks.

Meanwhile, the adiabatic flow assumption and constant temperature flow assumption are the most important simplifying assumptions employed for analyzing the natural gas flow inside pipelines. Analyzing the transient fluid flow of ideal compressible natural gas in a pipeline requires flow equations and implementing simplifying assumptions (such as one-dimensional isothermal flow and stable friction ratio) with reasonable errors [25]. After neglecting convective acceleration and simplifying two conservation equations (mass and energy), the following equations are obtained representing the relation of pressure and flow through horizontal pipelines.

A common method is to apply the Euler finite difference technique to replace the derivative expression both in space and time. Thus, the PDEs can be transformed into a set of algebraic equations at \((x, t)\) with time and spatial steps [26].

\[
\frac{\partial p}{\partial t} + \frac{p a^2}{A} \frac{\partial Q}{\partial x} = 0 \tag{1}
\]

\[
\frac{\partial Q}{\partial t} + \frac{A \partial p}{\rho} + \frac{2q_f Q |Q|}{DA} = 0 \tag{2}
\]

For dynamic equations of natural gas transmission, a method has been proposed based on simulation with electricity so as to follow the well-established methods of solving electric circuits for conquering the differential equations more easily [27]. Various models describe the dynamic behavior of natural gas flow using the analogy between natural gas network and electrical network [28]. Using the analogy of voltage and current in an electrical network with pressure and flow rate in the natural gas network, lead to the electrical elements will be derived as listed in Table I [29].

Changes of flow rate depend on fluid compressibility. So, in order to consider the capacitor properties of a pipeline, the relationship between pressure, flow rate and capacity is deemed as the relationship between voltage and current within an electrical capacitor, where the current is proportionate to the incremental change of voltage.

The capacity effect of a pipeline network and changes in a pipeline flow rate depend on the fluid compressibility. Accordingly, the equivalent pipeline capacity is obtained as follow [30]:

\[
C = \frac{\pi r^2 l}{\rho c^2} \tag{3}
\]

As (2) represents, pressure drop inside the pipeline might be caused by the following two factors. First, the pressure loss results from acceleration of a certain fluid mass, similar to an inductance effect in electric circuits. Second, the pressure drop might be related to frictional resistance of the pipeline. Therefore, the total pressure drop along a pipe is determined by both the resistance effect and the inductance effect. The relationship between the pressure drop and the flow change is similar to that of voltage and current at both ends of an electrical inductance [31].

Thus, the equivalent inductance of pipeline is modeled as:

\[
L = \frac{\rho |I|}{\pi r^2} \tag{4}
\]

Resistance estimation of a pipeline depends on the friction factor coefficient. There are several prevalent equations in the fully turbulent flow regime to estimate the Darcy friction factor, leading to distinct resistance models as presented in [32]. Moreover, the relationship between resistance and pressure drop in the pipeline conforms to Ohm’s law. If the Weymouth friction factor is used, the resistance of a compressible fluid distribution system has the following form:

\[
R = R(Q, \pi) = 0.6579 \times 10^{-11} \frac{T S z Q l}{D^3 (\pi_1 + \pi_2)} \tag{5}
\]

where the natural gas density is usually conceived as 0.7165 kg/m³. In the steady state of an electric circuit, the effects of capacitors and inductors are ignored and only resistors are considered, which means capacitors and inductances are equivalent to open and closed switches, respectively. The Weymouth equation could be obtained from such an equivalent circuit of pipelines in the steady state.

Like transmission lines in a power system, an equivalent circuit is defined for each pipeline of the natural gas transmission network so that similar methods can be utilized to solve the natural gas flow [33]. One example of the equivalent electric circuit for the transmission pipeline is presented in Fig. 1. Capacitors and inductors in the equivalent circuit indicate different time constants in the dynamic behavior of the fluid flow in pipelines due to the storage and compressibility of natural gas. The modeling of this equivalent circuit is obtained based on the steady state behavior of natural gas transmission network.

B. Transient behavior of natural gas network

Natural gas is transmitted from suppliers to consumers through transmission pipelines in a similar way to the delivery of power from power plants to consumers through transmission lines. However, different nature of natural gas and electricity leads to various differences in their transmission characteristics. Natural gas even has many transmission disparities with other fluids due to its compactness [34].

After the electricity transmission network, natural gas transmission networks are the second largest energy transmission networks in size.

### Table I

ANALOGY BETWEEN NATURAL GAS AND ELECTRICAL TRANSMISSION NETWORKS

<table>
<thead>
<tr>
<th>Electrical</th>
<th>Natural Gas</th>
</tr>
</thead>
<tbody>
<tr>
<td>Current, I</td>
<td>Flow, Q</td>
</tr>
<tr>
<td>Voltage, V</td>
<td>Pressure, (\pi)</td>
</tr>
<tr>
<td>Inductance, (L_e)</td>
<td>Fluid Inertia Constant, (L)</td>
</tr>
<tr>
<td>Resistance, (R_e)</td>
<td>Fluid resistance ratio, (R)</td>
</tr>
<tr>
<td>Capacitance, (C_e)</td>
<td>Pipe capacity and compressibility, (C)</td>
</tr>
</tbody>
</table>
However, due to compressibility properties of natural gas, natural gas networks are considered as the most complex non-linear systems in operation [35]. Also, natural gas power plants are the coupling points of these two largest energy transmission networks. Moreover, the operating condition of each network affects the other so that it is necessary to study the two networks in an integrated manner. Given the equivalent circuit for transmission pipelines, the two networks can be modeled in a unified form but solved differently. As shown in Fig. 1, in this analogy between natural gas transmission pipelines and electricity elements, adding a natural gas power plant to one end of a pipeline is equivalent to enforcing a step input signal in the equivalent electrical circuit.

One of the assumptions about using the analogy between the power transmission network and the natural gas pipeline is that each change in the pressure and flow of the pipelines is like a step-one function and other variable parameters will be calculated based on it. Indeed, the proposed model has no independency to time duration. If the flow at the end of natural gas transmission network is known as natural gas load independency to time duration. If the flow at the end of transmission networks. Moreover, the operating condition of thermal generating units is presented below:

\[
\begin{align*}
\lambda &= P_S - RQ_S \\
\beta &= \frac{2}{\sqrt{LC}} - \frac{R^2}{4L^2} \\
\gamma &= \frac{R}{2L} + \frac{2Q_S}{AC} \\
\mu &= \frac{RC}{L} \pi_S - 2Q_S \\
\chi &= \frac{4\pi_S - 2Q_SR}{L} \\
\varphi &= \frac{D}{C} \pi_S - \frac{R}{2L}
\end{align*}
\]

Finally, after transforming the Laplace equations in the frequency domain back to the time domain, we can obtain the transients of natural gas flow at the beginning of a pipe and pressure at its end.

\[
\begin{align*}
\pi_2(t) &= \lambda(u(t) - e^{\frac{R}{2\beta}} cos(\beta t) - \frac{\gamma}{\beta} sin(\beta t)) \\
Q_1(t) &= Q_S u(t) + \frac{\chi}{2\beta} e^{\frac{R}{2\beta}} cos(\beta t) + \frac{CP_S}{2} (e^{\frac{R}{2\beta}} cos(\beta t) - \frac{R}{2L\beta} e^{\frac{R}{2\beta}} sin(\beta t)) \\
&\quad \times (e^{\frac{R}{2\beta}} cos(\beta t) + \frac{\varphi}{\beta} e^{\frac{R}{2\beta}} sin(\beta t))
\end{align*}
\]

The following variables are defined for simplifying these equations:

\[
\begin{align*}
\pi_2 &= \frac{2\pi_S - 2(R + SL)Q_S}{S(LCS^2 + RCS + 2)} \\
Q_1 &= \frac{4YP_1(t) + 2Y^2P_2(t) + 4Q_2(t)}{4 + 2Y}
\end{align*}
\]

The start of a gas-fired unit in one side of a pipe could be modeled as a step-one input to the equivalent electrical circuit of the pipeline. According to this analogy, the transient behavior of the other variable is obtained in Eq. (17)-(18).

Based on these two equations, the dynamic behavior of natural gas transmission can be analyzed and observed parametrically. Sudden changes of the operating state in a pipe spread across the transmission network as a moment with the acoustic speed until the stabilization of all the pressure in the network. The exponential terms in the equations show the damping and response delay of the natural gas network.

IV. EXTENDED SECURITY CONSTRAINED UNIT COMMITMENT

A. Security-constrained unit commitment

Security-constrained unit commitment (SCUC) is widely used for minimizing power system operating costs while ensuring the security of the determined scheduling [36]. The SCUC is commonly formulated as a mixed integer programming problem subject to prevailing constraints in power system operations.

The objective function that minimize the cost of scheduling thermal generating units is presented below:
Min \sum_{l=1}^{L} \sum_{i=1}^{NG} \sigma_l (a_l P_{lt}^2 + b_l P_{lt} + c_l I_{lt} + SU_{lt}) + SD_{lt} + \sum_{l=1}^{T} \omega P_{LS} \tag{19}

Common operational and technical constraints include system energy balance, ramp up/down rate limits, system spinning/operating reserve requirements, system emission limits, unit output limits, min On/Off time limits, transmission line flow limits, emission limits, and fuel limits. Detailed formulation of SCUC and the related constraints are described in [37]. The nonlinear generation cost is linearized in the following equations:

\begin{align}
P_l = \sum_{i=1}^{L} \Delta P_l (l) \quad \forall i \\
o \leq \Delta P_l (l) & \leq \frac{P_{l_{\text{max}}}}{L} \quad \forall i, l = 1, 2, \ldots, L \tag{20} \\
CG_l = \sum_{i=1}^{L} k_l (\Delta P_l (l) + c) \quad \forall i \tag{21} \\
k_l (l) = (2l - 1) a_l \left( \frac{P_{l_{\text{max}}}}{L} \right) + b_l \quad \forall i, l = 1, 2, \ldots, L \tag{22} \\
\end{align}

Spinning reserve limits:

\begin{align}
\sum_{i=1}^{L} P_{l_{\text{min}}} I_{lt} \geq P_{D_t} + R_t \tag{24} \\
\end{align}

Ramping rate limits:

\begin{align}
P_{lt} - P_{lt+1} & \leq DR_t (1 - n_{lt}) + n_{lt} P_{l_{\text{max}}} \quad \forall i, \forall t \tag{25-a} \\
P_{lt+1} - P_{lt} & \leq UR_t (1 - f_{lt}) + f_{lt} P_{l_{\text{min}}} \quad \forall i, \forall t \tag{25-b} \\
\end{align}

Max/min generation output:

\begin{align}
P_{l_{\text{min}}} I_{lt} \leq P_{lt} \leq P_{l_{\text{max}}} I_{lt} \tag{26} \\
\end{align}

Minimum ON time constraints:

\begin{align}
f_{lt} \leq I_{lt+TD_{(l,e)}} \quad \forall i, \forall t \tag{27-a} \\
\end{align}

Where, TU (i,e) is presented as follows:

\begin{align}
TU (i,e) = \begin{cases} 
e & e \leq T_{on} \\
0 & e > T_{on} \\
\end{cases} \quad \forall i \\
\end{align}

Minimum OFF-time constraints:

\begin{align}
n_{lt} + I_{lt+TD_{(l,e)}} \leq 1 \quad \forall i, \forall t \tag{28-a} \\
\end{align}

Where TD (i,e) is presented as follows:

\begin{align}
TD (i,e) = \begin{cases} 
e & e \leq T_{off} \\
0 & e > T_{off} \end{cases} \quad \forall i \\
\end{align}

Natural Gas consumption constraint:

\begin{align}
a_l P_{lt}^2 + b_l P_{lt} + c_l I_{lt} \leq P_{l_{\text{max}}} \quad \forall i, \forall t \tag{29} \\
\end{align}

As objective function, this equation will be linearized according to (20)-(23).

Power transmission constraint in normal conditions:

\begin{align}
a_{pq} (\theta_{p,t} - \theta_{q,t} - \gamma_{p,q,t}) \leq MxFlow_{ma} \quad \forall m, (p,q \in m), t \tag{30} \\
\end{align}

Power transmission constraint in contingency conditions:

\begin{align}
a_{pq} (\theta_{p,t} - \theta_{q,t} - \gamma_{p,q,t}) \leq MxFlow_{ma} \quad \forall m, (p,q \in m), j, t \tag{31} \\
\end{align}

Contingencies are related to some lines and elements that have a dominant effect on the operation and topology of the power system and they could be single or multi-contingency based on the importance of the element and according to the related experience about the operation of each power network.

B. Natural gas storage

There are two ways for compressible natural gas to be stored in transmission networks for future use during critical periods [38]: directly stored in pipelines or kept in alternative storage tanks. A model has been designed for optimizing the remaining natural gas volume in the transmission pipes, which in fact determines the difference between the input and output natural gas at the beginning and at the end of each natural gas pipe [39]. For achieving a higher modeling accuracy and coordinating the two natural gas storage options, we resort to using dynamic and transient-based modeling methods.

In order to maintain the security and smoothness of the steady state natural gas flow, large quantities of natural gas are stored in storage tanks. Only when a contingency occurs on a natural gas transmission pipeline in a peak period, those storage facilities are committed and added to the natural gas transmission network. Accordingly, natural gas storage is modeled as a temporary supplier of natural gas, whose output rate and storage volume are given as follows:

\begin{align}
E_{l,t+1} = E_{l,t} + Q_{in,t} - Q_{out,t} \times ER_{so} \quad \forall so, \forall t \tag{32} \\
E_{\text{min}} \leq E_t \leq E_{\text{max}} \quad \forall t \tag{33} \\
\end{align}

where the output rate limit and tank capacity are available from natural gas companies.

C. Compressor

A compressor is analogous to a transformer that changes the voltage level in power systems. A simplified modeling of compressors is available in [22], which determines the quantity of natural gas compressed at each node according to a specified compressor factor. So, the transmission matrix modeling the relation of output and input parameters of a compressor is presented in the following:

\begin{align}
\[ \pi (q) = \begin{bmatrix} \alpha & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} q_{l} \\ q_{r} \end{bmatrix} \] \tag{34} \\
\end{align}

For pipelines with compressors, the pressure at the incoming end can be lower than that at the outgoing end.

D. Natural gas transient modeling

Natural gas fuel limits are modelled in natural gas load flow constraints. The natural gas load flow equation based on electrical analogy is formulated as follows [19]:

\begin{align}
q_{k,y,t} = \text{sign} \left( \pi_{k,y,t}, \pi_{y,t} \right) \left( \pi_{k,y,t}^2 - \pi_{y,t}^2 \right) \quad \forall g_i (k,y) \in g_i(t) \tag{35} \\
\end{align}

As shown in Fig. 4, the total sum of all inputs and outputs at each natural gas node should be zero. Thus, the balance constraint of fluid flowing through pipelines at each natural gas node is represented in the following:

\begin{align}
\sum_{sup=1}^{SUP} Q_{sup} + \sum_{so=1}^{STO} Q_{so} - \sum_{d=1}^{DEM} GL_d & = \sum_{L=1}^{LLP} Q_L + \sum_{com=1}^{CPR} Q_{com} \quad \forall t \tag{36} \\
\end{align}
Other operation constraints of natural gas network include pressure limits of each node and output limit of natural gas suppliers as written below:

\[
\pi_{g_{\text{min}}} \leq \pi_g(t) \leq \pi_{g_{\text{max}}} \quad \forall g, \forall t \quad (37)
\]

\[
Q_{\text{sup_{min}}} \leq Q_{\text{sup}}(t) \leq Q_{\text{sup_{max}}} \quad \forall \text{sup}, \forall t \quad (38)
\]

\[
Q_{\text{out_{so_{min}}}}, Q_{\text{out_{so_{max}}} \leq \text{SR}_{\text{so}}} \quad \forall \text{so}, \forall t \quad (39)
\]

With the natural gas storage equations obtained in section III-B, transient overshoot of the network and damping time of each pipe can be calculated for evaluating the transient stability based on steady state values.

An identical behavior of the natural gas in the pipeline is shown in Fig. 3, where the outputs follow any change in the condition of the network without any unstable behavior and transient pressure drop. From the SCUC operator point of view, the definition of the decision variable to present a reliable scheduling in both the power system and the natural gas networks is more important than seeing the behavior of the planning during the power system and the natural gas networks is more important than seeing the behavior of the planning during time. So these decision variables for controlling the transient behavior are formulated in Eq. (40)-(43)-(45), being able to respond to any change in the condition of the network.

Natural gas networks never exhibit fluctuating transient behavior due to their physical structure and operation timescale; in most cases, instantaneous load changes result in pressure drop. Therefore, the frequency of transient response for modeling the dynamic behavior is considered zero.

Accordingly, transient state equations based on electrical analogy are simplified as follows:

\[
\beta = 0, \quad \frac{8L}{C} = R^2(\pi, Q) \quad (40)
\]

\[
\pi_2(t) = \lambda(u(t) - e^{-RQ/t} - \gamma e^{-RQ/t}) \quad (41)
\]

\[
Q_1(t) = Q_2u(t) + \frac{1}{2}\frac{R}{2L}e^{-RQ/t} + \frac{C}{2}(e^{-RQ/t} - e^{-2RQ/t}) \quad (42)
\]

which do not exhibit instantaneous pressure increase with undershoot considered in accordance with the real-life natural gas network operation. Furthermore, the existence of the exponential term and their time constants could show the amount of natural gas that has been stored in the pipelines, known as line pack effect.

On the other hand, SCUC is implemented hourly and each time period of scheduling is 1 hour. Steady state equations of a natural gas network are only valid when the network’s transient behavior is less than 1 hour so that we create another constraint on scheduling validity by controlling the time constant of transient state equations less than 1 hour (shown in Fig. 3, with red dashed line).

\[
\frac{3}{\tau} = \frac{6L_{\text{pip}_{\text{t}}}}{R_{\text{pip}_{\text{t}}}^2(\pi, Q)} \leq 3600 \quad \forall t, \forall \text{pip} \quad (43)
\]

Maximum pressure drop and transient flow of the natural gas network can be calculated in order to preserve the network security during transients. Specifically, the maximum pressure drop should be limited such that natural gas load variations do not cause significant transient nor instantaneous pressure drop for making the network operation unstable. The maximum transient pressure drop is represented as follows:

\[
T(\pi_{\text{min}}) = \frac{1}{\gamma} \frac{2L_{\text{pip}_{\text{t}}}}{R_{\text{pip}_{\text{t}}}^2(\pi, Q)} \quad \forall t, \forall \text{pip} \quad (44)
\]

\[
\pi_2(T_{\text{min}}) \geq \frac{1}{2} \pi_{\text{min}} \quad (45)
\]

To this end, constraints (40), (43), and (45) are added to the SCUC model to ensure transient security of the natural gas network pertinent to the obtained generation schedule.

**E. Complete solution process**

Cooperation between the ISO or the utility operator and natural gas transmission operators is based on the exchange of the information of industrial and residential gas load forecasting with service priorities, natural gas transmission parameters, and planned outage of natural gas pipelines with ISO that would execute the day-ahead SCUC. It will check the feasibility of the natural gas transmission system for serving the expected natural gas loads based on available natural gas resources.

Transient behavior of natural gas network is investigated based on steady state electrical analogy such as the transient resistance. In other words, after determining steady state behavior of the natural gas network, equivalent resistance is calculated by using steady state pressure and flow as well as parameters for determining transient behavior. In other words, allowed values for sudden overshoot or undershoot in the natural gas network and allowed time to stabilize the natural gas network after disturbance can also be added for controlling transient security of natural gas network.

The SCUC problem is MIP and the natural gas transmission system in the steady state and transient stability check is nonlinear.
The solution method includes two levels. The first level uses a GA algorithm to solve the natural gas network problem and the second level uses the CPLEX solver in order to solve the SCUC optimization problem. The first level is a heuristic method to solve the nonlinear problem of the gas network system. A mixed integer linear programming problem is associated with the second level of the optimization problem (SCUC problem). In the first level the natural gas allocated to gas-fired units are variables of the problem. The GA will provide an initial value for these variables that could cover all natural gas transmission network constraints based on other natural gas network input data, such as other gas loads. The allocated gas will be sent to the SCUC problem. The operation cost of the power network will be the first value of the objective function of the GA, and in the other levels the problem will change the natural gas allocation to gas-fired units to find the minimum operation cost. This process will be checked in some different hours of the gas network with different conditions to find the best solution. In this way, all of the chromosomes which are sent to the second level problem are feasible in the viewpoint of the gas network.

These two problems have been separated as mentioned in [9], while a genetic algorithm is used for the nonlinear equation of the natural gas system. Thus, generation schedules obtained from steady state Weymouth equations can be investigated under transient security constraints of the natural gas network to ensure their dynamic stability.

V. CASE STUDY

Performance of the proposed SCUC model has been tested on the IEEE 24-bus power system and Belgian 20-node natural gas transmission system. The topology of the integrated power and natural gas network is shown in Fig. 4.

The power system has 24 buses, 38 branches, 17 loads, and three natural gas-fired units; four oil-fired units, five photovoltaic units; and three hydro units. The natural gas network has 20 nodes, 21 pipelines, 2 suppliers, 4 storages, and 9 non-electrical loads. All domestic demands and commercial natural gas loads are prior to electrical gas loads and it is assumed that they have firm transport contracts. Natural gas power plants have interruptible transport contracts. Complete configuration details about the test network are available at [16].

In order to evaluate the efficiency of the proposed model with transient constraints of natural gas transmission, we consider three distinct cases and compare the resulting generation schedules. In the first case, SCUC is solved only using steady state constraints of natural gas network. In the second scenario, SCUC is solved using transient state constraints in addition to steady state constraints. Since the operation of natural gas networks is affected by uncertainties of renewable energy generation and sudden changes of natural gas flow; thus, in the last case, the penetration rate of renewable energy resources is increased to investigate the effect of transient equations, when SCUC is solved and analyzed during transients and steady states separately. All domestic demands and commercial natural gas loads are assumed with a higher priority to electrical natural gas loads. All of them which have firm transport contracts and the supply to natural gas power plants is interruptible.

Case 1: SCUC with Steady State Constraint of natural gas transmission

Daily operation cost of the power system with natural gas transmission constraints in steady state is 6.135841 M$. For this purpose, the generation size and population of GA are assigned to 100 and 250, respectively. The stall generation of 180 is used as stopping criterion, setting the objective function tolerance to 1%. The Gaussian is used as mutation function. The proposed model used a 2.63 GHz Intel processor with 4 GB of memory. The Gaussian is used as mutation function.

Case 2: SCUC with Steady State and Transient Constraint of natural gas transmission

The power system operation cost is 6.269804 M$ after solving the proposed model for natural gas load flow. After linearizing natural gas flow equations, obtained values (i.e., pressure, flow) are added to transient state constraints. If the transient constraints are met, final solution is obtained; otherwise, the SCUC model is solved again and generation schedules would be changed to obtain final solution of the problem.

Comparison of the generation schedules obtained from the first two cases is shown in Fig. 5.

As can be seen in Fig. 5, the introduction of transient state constraints reduces sudden changes to the least and natural gas network stability becomes less sensitive to load changes. Considering the inertia of natural gas in transmission network, this stable behavior contributes to the operational performance of the natural gas network in practice.
In Fig. 6, the generation schedule of Unit 5 is presented. As shown, transient constraints of natural gas network cause the power plant to use more natural gas from the natural gas stored in pipelines at some hours, but the power plant output is reduced at some hours because of the new transient state constraints. Comparison of total natural gas consumption in the power system with and without considering transient gas constraints is shown in Fig. 7. Natural gas consumption of power plants increases when transient behavior of natural gas network is considered, while the natural gas withdrawal from suppliers is approximately equal in these two cases. That is because the transient study models the natural gas stored in pipelines. Considering transient state constraints, the total amount of daily natural gas consumption in natural gas power plants reduces the sudden changes of hourly natural gas loads of these power plants (about a few percent’s in this case), which represents the volume of natural gas that would be stored in the natural gas pipelines.

**Case 3: SCUC with Steady State and Transient Constraint of natural gas transmission in large scale system**

Now the proposed method will be tested on a large-scale power system network linked to a natural gas transmission grid. A modified IEEE 118-bus system linked with 14 node natural gas transmission grid as shown in Fig. 8, and Fig. 9, respectively, is studied. The power system has 12 combined cycle units, 54 fossil units, 7 hydro units, 9 tap changing transformers, 186 branches, and 91 demand sides. The natural gas transmission has 12 pipelines, 14 nodes, and two compressors. The complete test data is given in [40]. It is assumed that generation of 1MBtu of electrical energy consumes 1 kilo cubic feet of natural gas. At first, SCUC is calculated with natural gas constraints based on Weymouth equations in steady state, then the model is extended with transient constraints of natural gas network. The results are compared in Fig. 10.

**VI. CONCLUSION**

A SCUC model with transient gas transmission network constraints was proposed in this paper to utilize the electrical analogy between power transmission line and natural gas flow in the pipeline. Accordingly, a new set of constraints are defined for the transient stability of natural gas network. In order to check the transient stability of the natural gas grid, steady state parameters of the natural gas network, such as pressure and flow of pipelines, are embedded in the proposed transient state constraints. Unlike other methods, our method avoids complex and time-consuming calculations in
large-scale systems for natural gas flow, especially in short-term operation planning of power systems, such as the day-ahead scheduling of thermal power plants. Case studies have demonstrated the effectiveness of the proposed model based on the IEEE test power system linked by the natural gas grid. Although this is an appropriate method for the large-scale natural gas transmission network, one of its most important advantages is that this method can be easily interfaced and linked with other prevalent optimization problems for power system operation. Furthermore, ramping model of the generator outputs and electricity demand could better depict the importance of the consideration of the transient study of the natural gas network. To increase the accuracy of the model, it is necessary to present the power system in dynamic mode or the time step of the UC should break down to less than 1 hour.

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